## **Exponential Functions**

| KNOW                      | DO                  | UNDERSTAND   |
|---------------------------|---------------------|--|
| Can recognize an          | Can build equations | Function Characteristics:                              |
| exponential as increasing | for exponentials    | The base is the rate of growth/decay, and the          |
| or decreasing from given  | given two points    | horizontal stretch is the length of one growth period. |
| points. Can identify the  | and the asymptote.  | The vertical stretch is how far from the asymptote you |
| asymptote from the graph. |                     | start and the vertical shift is the asymptote.         |
| Vocab & Notation          |                     |  |

- Exponential growth/decay
- Euler's number, e

Consider the geometric sequence  $(2^k)_{k \in \mathbb{Z}}$ . Plot it on the graph below.





And the important thing is that we can change from one base to another.

$$f(x) = 2^x = (e^{0.7})^x = e^{0.7x}$$

We'll talk more about this next tomorrow on finding that power for *e*, but right now just be comfortable that we can do this at least through guess and check and when you start doing calculus you will only want to work exclusively with base *e*.

For now, let's look to see how any exponential function could be defined by an arbitrary base.

Unit 4: Exponential Growth



We've looked at doing a horizontal stretch, now we want to add the three other transformations to the exponential.

Unit 4: Exponential Growth

$$f(x) = a \cdot b^{\frac{x-c}{T}} + d = a \cdot e^{k(x-c)} + d$$

After a transformation we will be in one of four situations:

- Increasing or decreasing
- Approaching the asymptote or approaching infinity



**Example**: Determine an equation in base *e* for the exponential that passes through the points (-2, 6) and (5, -6) and has a horizontal asymptote of y = -10.

