

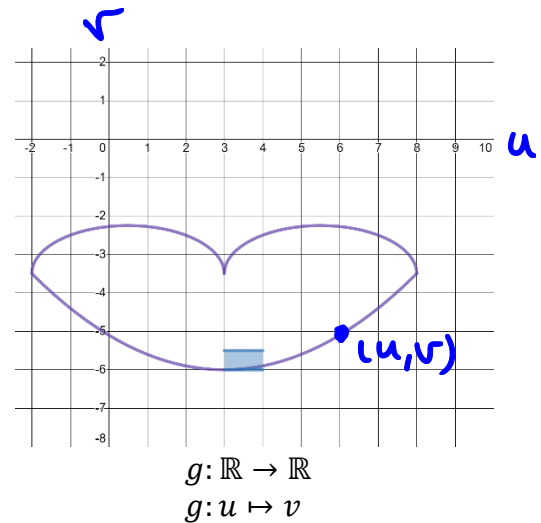
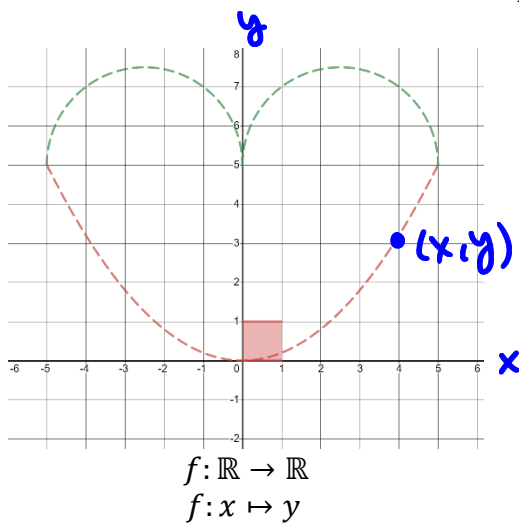
Function Translations

<p>KNOW Be able identify when a function was shifted left or right (and up or down) based on the mapping or function notation</p>	<p>DO Use Desmos and Geogebra to graph translations. Use correct mapping and function notation to describe a translation. Graph a translation accurately by hand. Determine the translation based on how points have moved.</p>	<p>UNDERSTAND <i>Transformations:</i> Can explain why translations left/right are opposite in function form. Can explain how vertical characteristics (range, y-intercepts, horizontal asymptotes) change by shifting up/down and how horizontal characteristics (domain, zeros and vertical asymptotes) change by shifting left/right</p>
<p>Vocab & Notation</p> <ul style="list-style-type: none"> • The plane of real numbers: \mathbb{R}^2 • Translation • Function Characteristics 		

We are going to be looking at how we can transform 2D space and functions that occupy space using mapping.

$$T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

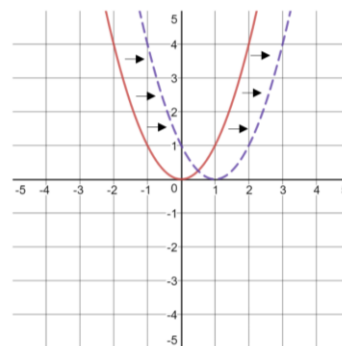
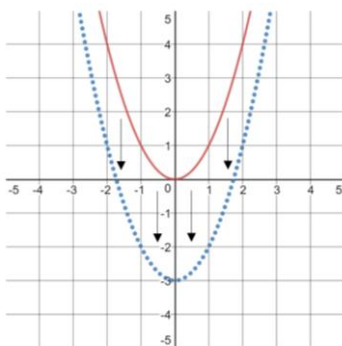
$$T: (x, y) \mapsto (u, v)$$



Definition: When a transformation moves 2D space horizontally and vertically this is called a **translation** and the mapping notation looks like:

$$T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

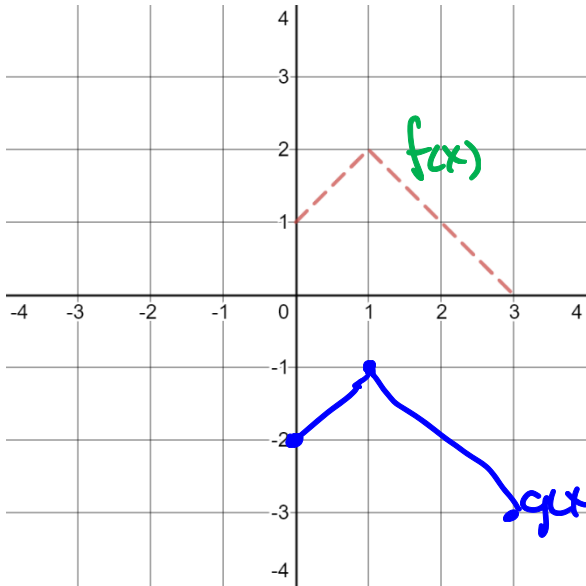
$$T: (x, y) \mapsto (x + c, y + d)$$



For a **vertical translation**, we shift space up and down and we apply the transformation:

$$T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

$$T: (x, y) \mapsto (x, y + d)$$



$$f: x \mapsto y$$

$$g: x \mapsto y + d$$

$$\Rightarrow y = f(x)$$

$$y + d = g(x)$$

$$g(x) = f(x) + d$$

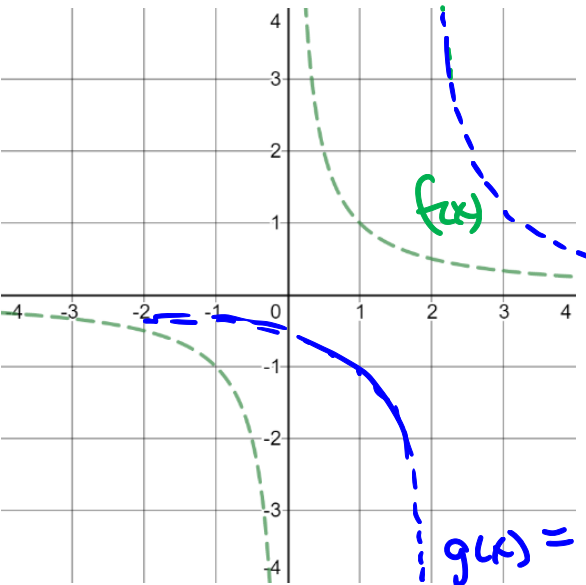
Example: $T: (x, y) \mapsto (x, y - 3)$ down 3 units

$$g(x) = f(x) - 3$$

For a **horizontal translation**, we shift the function left and right and apply the transformation:

$$T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

$$T: (x, y) \mapsto (x + c, y)$$



$$f: x \mapsto y$$

$$g: x + c \mapsto y$$

$$f(x) = y$$

$$g(x + c) = y = f(x)$$

$$\text{let } x + c = X \rightarrow g(X) = f(X - c)$$

Example: $T: (x, y) \mapsto (x + 2, y)$

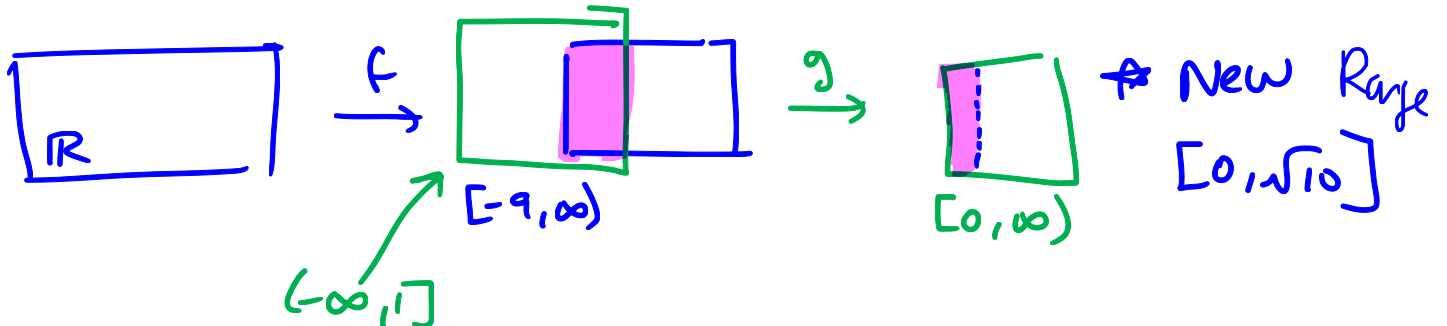
Right two units

$$g(x) = f(x - 2) \rightarrow \text{looks like its left!}$$

Composition Domain/Range Practice:

Given $f(x) = 2|x| - 9$ and $g(x) = \sqrt{1-x}$ determine the domain and range of $g \circ f$

$f: \mathbb{R} \rightarrow [-9, \infty)$ $g: (-\infty, 1] \rightarrow [0, \infty)$



* intersection is $[-9, 1]$

* Range take $x \in [-9, 1]$ → $-9 \leq x \leq 1$

$g(-9) = \sqrt{10}$

$g(1) = 0$

$9 \geq -x \geq -1$
 $10 \geq 1-x \geq 0$
 $\sqrt{10} \geq \sqrt{1-x} \geq 0$

~~Determine the domain and range of f, g~~

* Domain take $x \in \mathbb{R}$ Note $f(x) \in [-9, 1]$

⇒ $-9 \leq f(x) \leq 1$

$-9 \leq 2|x| - 9 \leq 1$

$0 \leq 2|x| \leq 10$

$0 \leq |x| \leq 5$ ⇒

New Domain $-5 \leq x \leq 5$

$g \circ f: [-5, 5] \rightarrow [0, \sqrt{10}]$

