Solving Sinusoidal Functions

KNOW

There are multiple solutions to a trig equation.

DO

Can find the solutions to a trig equation in a given domain. Can use special triangles when appropriate.

UNDERSTAND

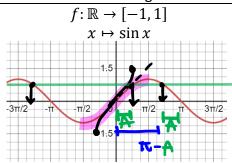
Inverse:

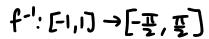
Sine and cosine are not 1-to-1 so the domain must be restricted. Restrictions come so that they take on all values of the range once.

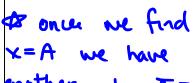
Vocab & Notation

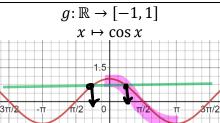
- $\arcsin x$, $\arccos x$, $\arctan x$
- = SIM 1x, cos x, ton 1x

Note how the domain gets restricted for the inverse functions:

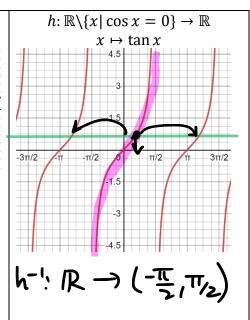








$$\Rightarrow$$
 so if $x=A$



Example

$$arcyn$$
 ($sin x = 0.8$

$$\Rightarrow X = 2.214 + 2\pi n$$
of
$$= 0.927 + 2\pi n, n6$$

$$axx = 0.8$$

oreton
$$(tm x = 0.8)$$

ne Z

Example (With Calculator) Use algebra to solve the following trig equations:

$$\frac{1}{2}\sin(\pi(x-0.1)) = 0.2$$

$$\Rightarrow \theta = 0.412 + 2\pi n$$

$$\Rightarrow \cos(x) \left(\sin\theta = 0.4\right)$$

$$\Rightarrow \cot(x-0.1) = 0.412 \text{ or } 2.730 + 2\pi n$$

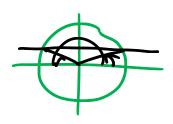
$$\Rightarrow \cot(x-0.1) = 0.412 \text{ or } 2.730 + 2\pi n$$

$$\Rightarrow \cot(x-0.1) = 0.412 \text{ or } 0.869 + 2n$$

$$\Rightarrow \cot(x-0.1) = 0.131 \text{ or } 0.869 + 2n$$

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Example (Without Calculator)

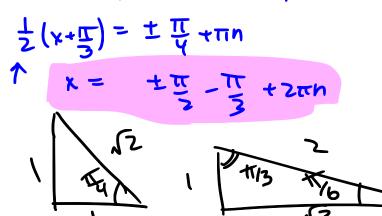
$$\left(\tan^{2}\left(\frac{1}{2}(x+\frac{\pi}{3})\right)-1\right)\left(2\cos\left(\frac{x}{3}\right)+1\right)=0 = \left(\tan^{2}\theta-1\right)\left(2\cos\varphi+1\right)$$

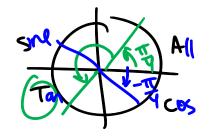
$$=0 = 0$$

$$\tan^{2}\theta=1 \quad \text{or} \quad \cos\varphi=\frac{1}{2} \quad \Rightarrow \quad \text{phi} \quad \varphi=\pm\frac{2\pi}{3}+2\pi n \quad \varphi \quad \varphi$$

$$+\cos\theta=\pm1 \quad \qquad \frac{x}{3}=\pm\frac{2\pi}{3}+2\pi n \quad \varphi \quad \varphi \quad \Rightarrow \quad \varphi = \frac{1}{2}$$

$$\theta=\frac{\pi}{4}+\pi n \quad \text{or} \quad -\frac{\pi}{4}+\pi n \quad \qquad x=\pm2\pi+6\pi n$$







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Practice:

$$2\sin^2 x - 3\sin x + 1 = 0$$



$$2\cos\left(\frac{\pi}{5}(x-3)\right) + 1 = 0.5$$



$$\tan^2 2x + 4\tan 2x - 5 = 0$$

$$4\cos^3\left(\frac{\pi}{4}(x+1)\right) = 3\cos\left(\frac{\pi}{4}(x+1)\right)$$

$$\csc^2\left(\frac{3}{5}\left(x - \frac{\pi}{2}\right)\right) = 4$$

$$\sec^2\left(\frac{\pi}{12}(x+3)\right) = 2$$

$$\frac{2}{3}\sec\left(\frac{\pi}{5x}\right) = 1$$

$$5\cot\left(\frac{x^2}{6}\right) - 3 = 0$$