

Week 4 Derivative Rules Review

Name _____

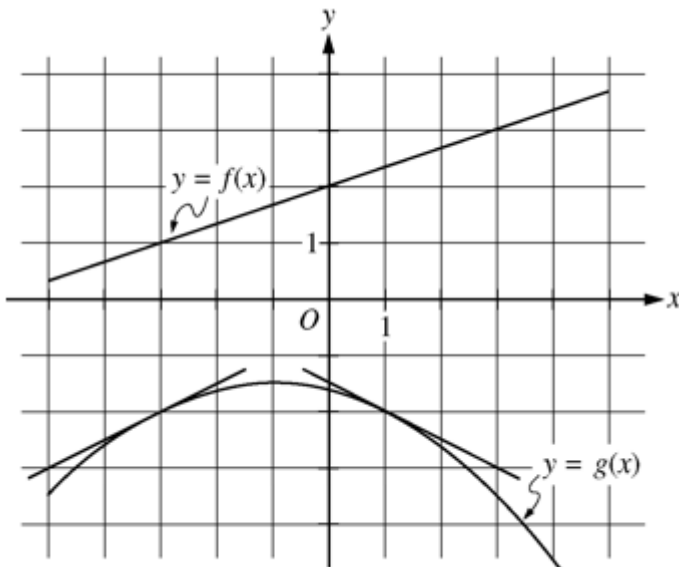
1.

x	3	7
$h(x)$	7	22
$h'(x)$	5	10

Selected values of the increasing function h and its derivative h' are shown in the table above. If g is a differentiable function such that $h(g(x)) = x$ for all x , what is the value of $g'(7)$?

- (A) $-1/10$
- (B) $1/10$
- (C) $1/5$
- (D) $7/5$

2.



The figure above shows the graphs of the functions f and g . The graphs of the lines tangent to the graph of g at $x = -3$ and $x = 1$ are also shown. If $B(x) = g(f(x))$, what is $B'(-3)$?



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(A) $-\frac{1}{2}$

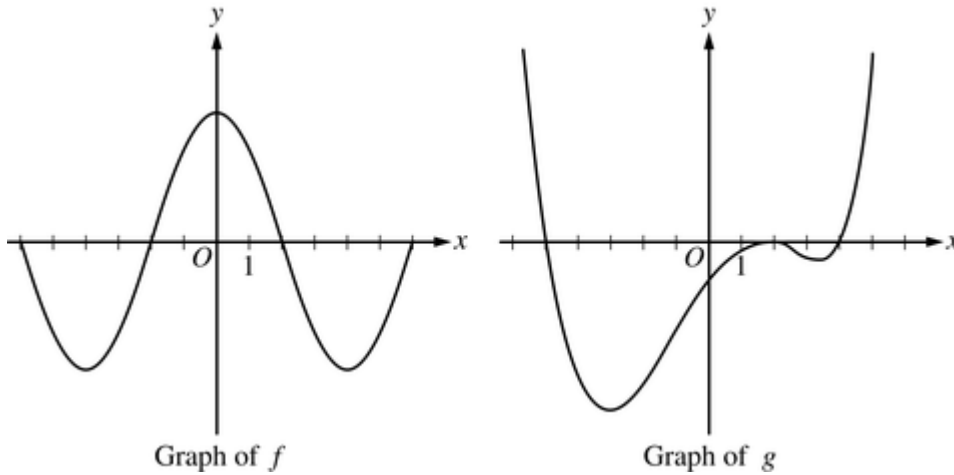
(B) $-\frac{1}{6}$

(C) $\frac{1}{6}$

(D) $\frac{1}{3}$

(E) $\frac{1}{2}$

3.



The graphs of two differentiable functions f and g are shown above. Given $p(x) = f(x)g(x)$ which of the following statements about $p'(-2)$ is true?



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- (A) $p'(-2) < 0$
- (B) $p'(-2) = 0$
- (C) $p'(-2) > 0$
- (D) $p'(-2)$ is undefined.
- (E) There is not enough information given to conclude anything about $p'(-2)$.

4. If $y = \arctan(e^{2x})$, then $\frac{dy}{dx} =$

- (A) $\frac{2e^{2x}}{\sqrt{1-e^{4x}}}$
- (B) $\frac{2e^{2x}}{1+e^{4x}}$
- (C) $\frac{e^{2x}}{1+e^{4x}}$
- (D) $\frac{1}{\sqrt{1-e^{4x}}}$
- (E) $\frac{1}{1+e^{4x}}$

5. If g is the function given by $g(x) = \frac{1}{3}x^3 + \frac{3}{2}x^2 - 70x + 5$, on which of the following intervals is g decreasing?



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(A) $(-\infty, -10)$ and $(7, \infty)$

(B) $(-\infty, -7)$ and $(10, \infty)$

(C) $(-\infty, 10)$

(D) $(-10, 7)$

(E) $(-7, 10)$

6.  Let f be the function given by $f(x) = \cos(2x) + \ln(3x)$. What is the least value of x at which the graph of f changes concavity?

(A) 0.56

(B) 0.93

(C) 1.18

(D) 2.38

(E) 2.44

7. If $f(x) = \frac{5-x}{x^3+2}$, then $f'(x) =$




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(A) $\frac{-4x^3 + 15x^2 - 2}{(x^3 + 2)^2}$

(B) $\frac{-2x^3 + 15x^2 + 2}{(x^3 + 2)^2}$

(C) $\frac{2x^3 - 15x^2 - 2}{(x^3 + 2)^2}$

(D) $\frac{4x^3 - 15x^2 + 2}{(x^3 + 2)^2}$

8.  Let $f(x) = \int_0^{x^2} \sin t \, dt$. At how many points in the closed interval $[0, \sqrt{\pi}]$ does the instantaneous rate of change of f equal the average rate of change of f on that interval?

(A) Zero

(B) One

(C) Two

(D) Three

(E) Four

9.

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
0	3	4	2	π

The table above gives values of the differentiable functions f and g and their derivatives at $x = 0$. If $h(x) = \frac{f(x)}{g(x)}$, what is the value of $h'(0)$?



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(A) $\frac{8-3\pi}{4}$

(B) $\frac{3\pi-8}{4}$

(C) $\frac{4}{\pi}$

(D) $\frac{2-3\pi}{2}$

(E) $\frac{8+3\pi}{4}$

10. If $y = \tan x - \cot x$, then $dy/dx =$

(A) $\sec x \csc x$

(B) $\sec x - \csc x$

(C) $\sec x + \csc x$

(D) $\sec^2 x - \csc^2 x$

(E) $\sec^2 x + \csc^2 x$

11. An equation of the line tangent to the graph of $f(x) = x(1 - 2x)^3$ at the point $(1, -1)$ is



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(A) $y = -7x + 6$

(B) $y = -6x + 5$

(C) $y = -2x$

(D) $y = 2x - 3$

(E) $y = 7x - 8$

12. If $f(x) = \ln x$, then $\lim_{x \rightarrow 3} \frac{f(x) - f(3)}{x - 3}$ is

(A) $\frac{1}{3}$

(B) e^3

(C) $\ln 3$

(D) nonexistent

13. If $\ln(2x + y) = x + 1$, then $\frac{dy}{dx} =$



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- (A) -2
- (B) $2x + y - 2$
- (C) $2x + y$
- (D) $4x + 2y - 2$
- (E) $y - \frac{y}{x}$

14. Suppose that f is an odd function; i.e., $f(-x) = -f(x)$ for all x . Suppose that $f'(x_0)$ exists. Which of the following must necessarily be equal to $f'(-x_0)$?

- (A) $f'(x_0)$
- (B) $-f'(x_0)$
- (C) $\frac{1}{f'(x_0)}$
- (D) $-\frac{1}{f'(x_0)}$
- (E) None of the above

15. If $y = x^2 e^x$, then $\frac{dy}{dx} =$



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(A) $2xe^x$

(B) $x(x + 2e^x)$

(C) $xe^x(x + 2)$

(D) $2x + e^x$

(E) $2x + e$

16. If $x^2 + xy - 3y = 3$, then at the point $(2, 1)$, $\frac{dy}{dx} =$

(A) 5

(B) 4

(C) $\frac{7}{3}$

(D) 2

17. If $f(x) = x^2 + 2x$, then $\frac{d}{dx}(f(\ln x)) =$



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- (A) $\frac{2 \ln x + 2}{x}$
- (B) $2x \ln x + 2x$
- (C) $2 \ln x + 2$
- (D) $2 \ln x + \frac{2}{x}$
- (E) $\frac{2x+2}{x}$

18. If $f(x) = (x - 1)^2 \sin x$, then $f'(0) =$

- (A) -2
- (B) -1
- (C) 0
- (D) 1
- (E) 2

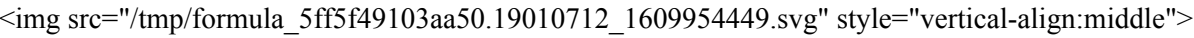
19. If f is a differentiable function and $y = \sin(f(x^2))$ what is $\frac{dy}{dx}$ when $x = 3$?



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(A) $\cos (f'(9))$

(B) $6\cos (f(9))$

(C) 

(D) $(6f'(9))\cos(f(9))$

20. Let f be the function defined by $f(x) = 2x + e^x$. If $g(x) = f^{-1}(x)$ for all x and the point $(0, 1)$ is on the graph of f , what is the value of $g'(1)$?

(A) $\frac{1}{2+e}$

(B) $\frac{1}{3}$

(C) $\frac{1}{2}$

(D) 3

(E) $2 + e$

21. Let f be the function defined by $f(x) = x^3 + x$. If $g(x) = f^{-1}(x)$ and $g(2) = 1$, what is the value of $g'(2)$?



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(A) $\frac{1}{13}$

(B) $\frac{1}{4}$

(C) $\frac{7}{4}$

(D) 4

(E) 13

22. Let f be a differentiable function such that $f(3) = 15$, $f(6) = 3$, $f'(3) = -8$, and $f'(6) = -2$. The function g is differentiable and $g(x) = f^{-1}(x)$ for all x . What is the value of $g'(3)$?

(A) $-\frac{1}{2}$

(B) $-\frac{1}{8}$

(C) $\frac{1}{6}$

(D) $\frac{1}{3}$

(E) The value of $g'(3)$ cannot be determined from the information given.

23. $\frac{d}{dx}(\tan^{-1}x + 2\sqrt{x}) =$



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(A) $-\frac{1}{\sin^2 x} + \frac{1}{\sqrt{x}}$

(B) $\frac{1}{\sqrt{1-x^2}} - 4\sqrt[3]{x}$

(C) $\frac{1}{\sqrt{1-x^2}} + \frac{1}{\sqrt{x}}$

(D) $\frac{1}{1+x^2} - 4\sqrt[3]{x}$

(E) $\frac{1}{1+x^2} + \frac{1}{\sqrt{x}}$

24. If $\arcsin x = \ln y$, then $\frac{dy}{dx} =$

(A) $\frac{y}{\sqrt{1-x^2}}$

(B) $\frac{xy}{\sqrt{1-x^2}}$

(C) $\frac{y}{1+x^2}$

(D) $e^{\arcsin x}$

(E) $\frac{e^{\arcsin x}}{1+x^2}$

25. The function h is given by $h(x) = x^5 + 3x - 2$ and $h(1) = 2$. If h^{-1} is the inverse of h , what is the value of $(h^{-1})'(2)$?



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(A) $\frac{1}{83}$

(B) $\frac{1}{8}$

(C) $\frac{1}{2}$

(D) 1

(E) 8

26. What is the slope of the line tangent to the curve $y = \arctan(4x)$ at the point at which $x = \frac{1}{4}$?

(A) 2

(B) $\frac{1}{2}$

(C) 0

(D) $-\frac{1}{2}$

(E) -2

27. If $\lim_{h \rightarrow 0} \frac{\arcsin(a+h) - \arcsin(a)}{h} = 2$, which of the following could be the value of a ?



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
(A) $\frac{\sqrt{2}}{2}$

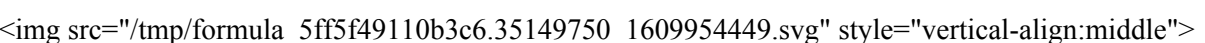
(B) $\frac{\sqrt{3}}{2}$

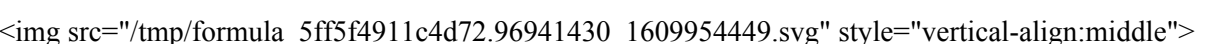
(C) $\sqrt{3}$

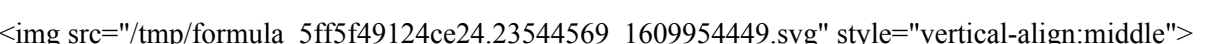
(D) $\frac{1}{2}$

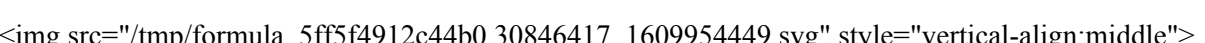
(E) 2

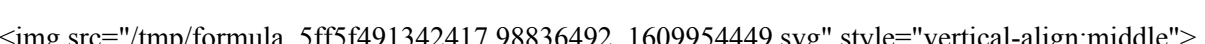
28. An equation for a tangent to the graph of  at the origin is

(A) 

(B) 

(C) 

(D) 

(E) 

29. If $\frac{dy}{dx} = x^4 - 2x^3 + 3x - 1$, then $\frac{d^3y}{dx^3}$ evaluated at $x=2$ is



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(A) 11

(B) 24

(C) 26

(D) 125

30. If $x^2+y^2=25$, what is the value of $\frac{d^2y}{dx^2}$ at the point (4,3) ?

(A) $-\frac{25}{27}$

(B) $-\frac{7}{27}$

(C) $\frac{7}{27}$

(D) $\frac{3}{4}$

(E) $\frac{25}{27}$